

Relation b/w Conduction Current density & Displacement

Current Density :- for a medium having conductivity σ & permittivity ϵ then

$$\vec{J}_c = \sigma \vec{E}$$

$$\vec{J}_d = \epsilon \frac{\partial \vec{E}}{\partial t}$$

If we incident a electromag. wave over such a medium

then

$$\vec{J}_c = \sigma \vec{E}$$

$$\vec{J}_d = \epsilon(-i\omega)\vec{E}$$

$$\vec{E} = E_0 e^{i(kz - \omega t)} \hat{x}$$

Then

$$\frac{J_c}{J_d} = \frac{\sigma}{\epsilon(-i\omega)}$$

$$\left| \frac{J_c}{J_d} \right| = \left| \frac{\sigma}{\omega \epsilon} \right|$$

for Good conductor, $\frac{\sigma}{\omega \epsilon} \gg 1$

$$\text{so } \boxed{J_c \gg J_d}$$

for Poor conductor, σ is less $\frac{\sigma}{\omega \epsilon} \ll 1$

$$\text{so } \boxed{J_c \ll J_d}$$

{ e.g. for a metal, $J_c = 10^6 \text{ A/m}^2$ & $J_d = 10 \text{ A/m}^2$ then }
it is Good conductor.

If $\sigma \uparrow$ then $J_c \uparrow$ (more)

If $\epsilon \uparrow$ or $\omega \uparrow$ then $J_d \uparrow$

i.e. $J_c \rightarrow$ depend on conductivity

$J_d \rightarrow$ " " permittivity & freq.