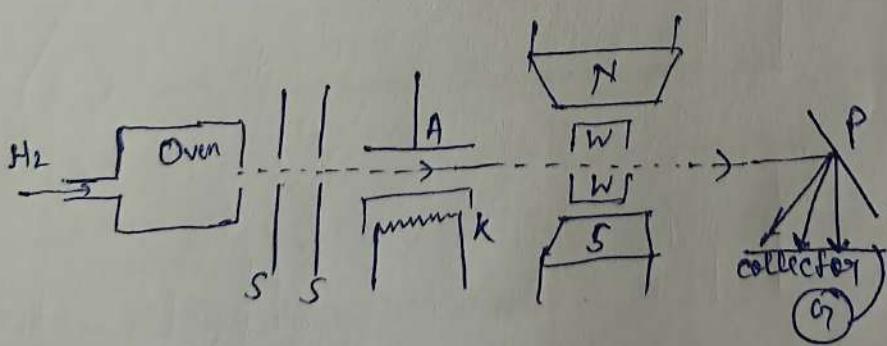


R.C. William studied the fine structure of H_d & D_d lines extensively using triple-prism spectrophotograph and a micro-photometer. There were two main differences between theory and experiment.

- (a) The component I_a was observed weaker than II_b which is in contradiction with theory. II_b was observed to be stronger than as predicted by the theory. This may be due to unequal excitation of the level $n=3$.
- (b) Separation between I_a & II_b was observed to be 0.319 cm^{-1} against theoretical separation 0.329 cm^{-1} . Similarly the separation between II_b & III_b was observed to be 0.134 cm^{-1} instead of 0.108 cm^{-1} .

Lamb shift: \rightarrow Lamb & Rutherford in 1947 performed a microwave experiment on Hydrogen atom & showed that for hydrogen-like atoms the states of a particular n values having terms with the same j value but different l values such as $2^2P_{3/2}$ & $2^2S_{1/2}$ are not degenerate but are separated. This separation is known as Lamb shift.

Experimental arrangements: \rightarrow



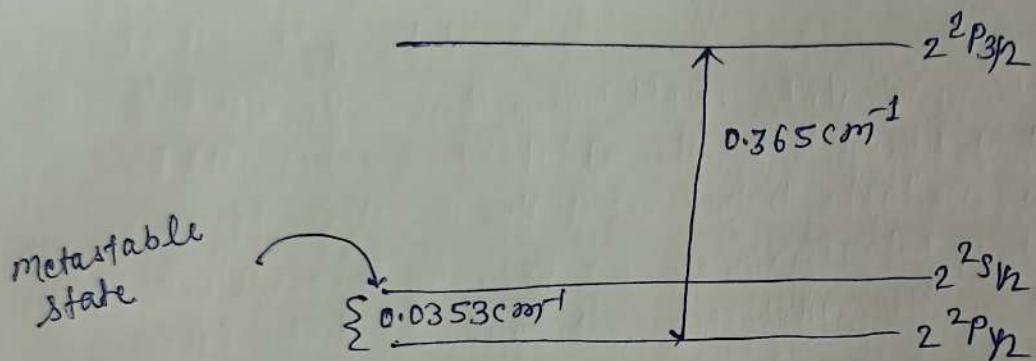
The experimental arrangement of Lamb-Rutherford experiment is shown in the above figure.

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- (a) Molecular hydrogen H_2 enters into the oven was dissociated into atom allowed to leave oven and passed through slits S, S.
- (b) This beam of hydrogen atoms passed through a vacuum diode in which electrons were emitted from cathode K and accelerated towards anodes.
- (c) some of the normal atoms ($1^2S_{1/2}$) passing through this region collided with the electrons and were excited to $2^2S_{1/2}$, $2^2P_{3/2}$ & $2^2P_{1/2}$ states.
- (d) These excited atoms moved towards the tungsten plate P and collide with this plate. During this the atoms in $2^2P_{3/2}$ & $2^2P_{1/2}$ states returned to the $1^2S_{1/2}$ state.
- (e) But the atoms in the metastable state $2^2S_{1/2}$ do not return to $1^2S_{1/2}$ as $\Delta E \neq 0$. These metastable atoms returned to their ground state through collision with P from which electrons were emitted.
- (f) Now these streams of e⁻s were collected and passed to a galvanometer which measures the metastable atomic beam intensity.
- (g) Mechanism causes metastable $2^2S_{1/2}$ atoms to make transition to $2^2P_{3/2}$ will result fall in the galvanometer reading i.e. fall in galvanometer reading is sensitive to the metastable atoms.
- (h) Metastable atoms transition were induced by passing the atoms through the waveguide WHI which creates microwaves of variable frequency.
- (i) At certain frequency the metastable atomic beam intensity suddenly reduced. It was due to absorption of microwave frequency by $2^2S_{1/2}$ atoms which were excited to the $2^2P_{3/2}$ state from which these atoms come to the ground state.

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- (j) The atoms reaching the tungsten plate were in their ground state and could not eject electron from it. Therefore the frequency was measure of the form difference between $2^2S_{1/2}$ & $2^2P_{3/2}$ states. This difference was not 0.365cm^{-1} but less (0.0353cm^{-1}).
 (k) Instead of adjusting the frequency of microwave for maximum reduction in the metastable atomic beam intensity. The energy levels can be adjusted by means of magnet NS.



Groundstate $1^2S_{1/2}$

Q.1. The doublet splitting for the first excited state $2P_{1/2} - 2P_{3/2}$ of hydrogen atom is 0.365cm^{-1} . Calculate the corresponding splitting for Ne^+ .

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Hyperfine structure of spectral lines :-

Under highest possible ~~in~~ resolution instrument fine structure components of spectral lines further splitted into components of separation of the order 1 cm^{-1} . This is very much smaller than the ordinary multiplet structure. This splitting is caused by atomic nucleus and is termed as 'Hyperfine structure'.

There are two types of nuclear effects which produces hyperfine structure.

- ① Isotope effect ② Nuclear spin & Hyperfine splitting.

① Isotope effect: →

* — Isotope: — The element having same atomic number with different mass number is called isotope. example, ${}^{1}_H$, ${}^{2}_H$, ${}^{3}_H$.

Nuclear mass is present in the Rydberg's constant for an atom. Different isotopes have different values of Rydberg's constant. The same transitions in different isotopes give rise to slightly different wave numbers.

example: First four members of Balmer series $H\alpha$, $H\beta$, $H\gamma$ & $H\delta$ has a very weak companion on the short wavelength side at distance 1.79 , 1.33 , 1.19 & 1.12 \AA respectively.

$H\beta = 4861.33 \text{ \AA}$ we have to calculate shift for this line for ${}^{2}_H$ — ${}^{1}_D$

$$\text{we know that } \frac{1}{\lambda_H} = R_H \left[\frac{1}{2^2} - \frac{1}{4^2} \right] \quad \dots \textcircled{1}$$

$$\frac{1}{\lambda_D} = R_D \left[\frac{1}{2^2} - \frac{1}{4^2} \right] \quad \dots \textcircled{2}$$

$$\frac{\lambda_D}{\lambda_H} = \frac{R_H}{R_D} \quad \dots \textcircled{3}$$

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(65)

Time: 01 P.M.

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$$\frac{\lambda_D - \lambda_H}{\lambda_H} = \frac{R_H - R_D}{R_D} , \quad \Delta \lambda = \lambda_D - \lambda_H$$

$$\Delta \lambda = \lambda_D - \lambda_H = -\lambda_H \left[\frac{R_D - R_H}{R_D} \right] = -4861.33 \text{ Å} \left[\frac{109707 \text{ cm}^{-1} - 109677.6 \text{ cm}^{-1}}{109707.4 \text{ cm}^{-1}} \right]$$

$$\boxed{\Delta \lambda = -1.32 \text{ Å}}$$

Note: → In the heavy atoms the main contribution to isotope shift is not due to difference in mass but due to change in nuclear radius with mass & deviation of the nuclear magnetic field from being purely a coulombian one.