

\downarrow Determination of spectral term for L-S coupling! →

example (a) Atoms with one optical electron i.e 1s
Here $l=0, s=\frac{1}{2}$, $S=2s+1 = 2 \times \frac{1}{2} + 1 = 2$
 $J=(l+s)=\frac{1}{2}$

$$\Rightarrow \text{Term value} = {}^{2s+1} A_J = {}^2 S_{1/2} \quad \text{as } l=0 \Rightarrow S \text{ state}$$

(b) Atom with two non equivalent optical electron
Non-equivalent e⁻ have different 'n' & l value.

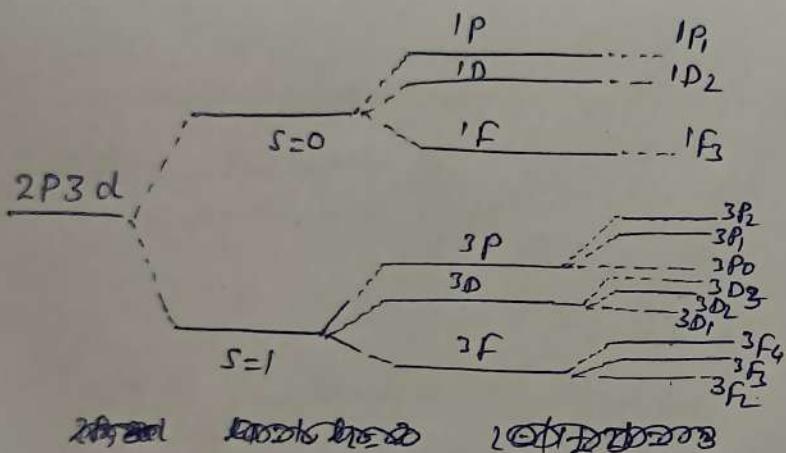
$$2p\ 3d \rightarrow l_1=1, \ l_2=2, \ s_1=\frac{1}{2}, \ s_2=\frac{1}{2}$$
$$J=(s_1+s_2)=0, 1 \quad S=2s+1 = 2 \times 0 + 1 = 1 \quad (\text{singlet})$$
$$= 2 \times 1 + 1 = 3 \quad (\text{triplet})$$

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$$l_1 = 1, l_2 = 2 \quad L = |l_1 + l_2| = 1, 2, 3 \quad (P, D, F)$$

$$J = |L \pm S| = \begin{matrix} 1+0 = 1 \\ 2+0 = 2 \\ 3+0 = 3 \end{matrix} \quad S=0, 2S+1=1$$

$$\begin{matrix} J = & 2 \pm 1 = 1, 2, 3 \\ & 3 \pm 1 = 1, 2, 3, 4 \\ & 1 \pm 1 = 0, 1, 2 \end{matrix} \quad S=1$$



Non equivalent optical electrons :-

The electrons having different 'n' & 'l' values are known as non equivalent optical electrons e.g. $2P, 3d \quad n=2, 3, l=1, 2$

Equivalent optical electrons
The electrons having same value of 'n' & 'l' is known as equivalent electrons
e.g. $2P^2 \quad n=2, l=1$ for both of the optical e-

Degeneracy of level $2P3d$

Degeneracy is calculated with the formula $(2J+1)$

| | | |
|-------------------|------------|--------------------------------|
| for $1P_1, J=1$, | degeneracy | $= 2J+1 = 2 \times 1 + 1 = 03$ |
| $1D_2, J=2$ | " | $= 2J+1 = 2 \times 2 + 1 = 05$ |
| $1F_3, J=3$ | " | $= 2J+1 = 2 \times 3 + 1 = 07$ |
| $3P_2, J=2$ | " | $= 2J+1 = 2 \times 2 + 1 = 05$ |
| $3P_1, J=1$ | " | $= 2J+1 = 2 \times 1 + 1 = 03$ |
| $3P_0, J=0$ | " | $= 2J+1 = 2 \times 0 + 1 = 01$ |
| $3D_3, J=3$ | " | $= 2J+1 = 2 \times 3 + 1 = 07$ |
| $3D_2, J=2$ | " | $= 2J+1 = 2 \times 2 + 1 = 05$ |
| $3D_1, J=1$ | " | $= 2J+1 = 2 \times 1 + 1 = 03$ |
| $3F_4, J=4$ | " | $= 2J+1 = 2 \times 4 + 1 = 09$ |
| $3F_3, J=3$ | " | $= 2J+1 = 2 \times 3 + 1 = 07$ |
| $3F_2, J=2$ | " | $= 2J+1 = 2 \times 2 + 1 = 05$ |

Total degeneracy = 60

The degeneracy can be removed when an atom is placed in external magnetic field.

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- * closed subshell like s^2, p^6, d^{10}, f^{14} will give rise to 1S_0 term
- * closed subshell contains maximum number of electrons = $2(2l+1)$

example $s^2 \quad l=0, \text{ no of electrons} = 2(2 \times 0 + 1) = 2$
 $p^6 \quad l=1 \quad \dots \quad = 2(2 \times 1 + 1) = 2(3) = 6$

- * The term can be odd/even when $\sum l = \text{odd/even}$
- example $4p4d, l_1=1, l_2=2 \quad \sum l = 1+2 = 03 \text{ odd}$ then we can write the term as $'P^o, 'D^o, 'F^o, 3P^o, 3D^o, 3F^o$

Term value determination of equivalent e⁻s

Rule:- The terms of configuration $(nl)^q$ are same as the terms of the configuration $(nl)^{g_l-q}$ $g_l = \text{maximum number of e}^-$
 $g_l = 2(2l+1)$

Term of p^1 is similar to p^5 for p subshell $l=1$

p^2 is similar to p^{n-2} maximum no of $e^- = 2(2l+1)$
 $g_l = 2(2 \times 1 + 1)$
 $g_l = 6$

$q=1$ given $p^1 \dots p^{6-1} = p^5$

Term of p^1 is similar to p^5

Question ① p^2 is similar to --- ?

② d^2 is similar to --- ?

③ d^8 is similar to --- ?

④ p^4 is similar to --- ?

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Determination of term values for equivalent electrons: →

$(nd)^2$ n & l are same for both of the electrons hence these are termed as equivalent electrons.

$$S_1 = \frac{1}{2}, S_2 = \frac{1}{2} \quad S = S_1 \pm S_2 = 0, 1$$

$$l_1 = 2, l_2 = 2 \quad L = |l_1 \pm l_2| = 0, 1, 2, 3, 4$$

S, P, D, F, L

Now According to Bril's scheme the possible values of m is

| | | | | | | |
|-------|---|----|----|----|----|----|
| m_L | 2 | 1 | 0 | -1 | -2 | |
| M_L | 4 | 3 | 2 | -1 | 0 | 2 |
| M_L | 3 | 2 | 1 | 0 | -1 | 1 |
| M_L | 2 | 1 | 0 | -1 | -2 | 0 |
| M_L | 1 | 0 | -1 | -2 | -3 | -1 |
| M_L | 0 | -1 | -2 | -3 | -4 | -2 |

for $S=1, L=3 \& l=1$
 $S=0, L=4, 2, 0$

4, 3, 2, 1, 0, -1, -2, -3, -4 → $^1G, L=4$
3, 2, 1, 0, -1, -2, -3 → $^3F, L=3$
2, 1, 0, -1, -2 → $^1D, L=2$
1, 0, -1 → $^3P, L=1$
0 → $^3S, L=0$

Possible states are $^1G, ^3F, ^1D, ^3P, ^1S$

$$^1G \quad L=4, S=0 \Rightarrow ^1G_4 \quad ^3P, L=1, S=1 \quad T=1 \pm 1 = 0, 1, 2$$

$$^1D \quad L=2, S=2 \Rightarrow ^1D_2 \quad ^3P_{0,1,2}$$

$$^1S \quad L=0, S=0 \Rightarrow ^1S_0 \quad ^3F, \quad L=3, S=1, T=1 \pm 3 = 2, 3 \\ ^3F_{2,3,4}$$

The term value for $(nP)^2$ state will be $^1G_4, ^3F_2, ^3F_3, ^1D_2, ^3P_{0,1,2}, ^1S_0$

the terms of $(nP)^2$ will be similar to $(np)^4$

Therefore the terms of $(np)^4$ will be $^1G_4, ^3F_2, ^3F_3, ^1D_2, ^3P_{0,1,2}, ^1S_0$

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Determination of term value of $(nd)^2$ configuration:
 $(np)^2$ the electrons are equivalent as n is similar & $l=2$ for both the e^- 's.

$$S_1 = \frac{1}{2}, S_2 = \frac{1}{2} \Rightarrow S = |S_1 + S_2| = 0, 1$$

$$L_1 = 2, L_2 = 2 \Rightarrow L = |L_1 + L_2| = 0, 1, 2, \cancel{3, 4}$$

S.P.D. ~~for~~

possible MC values from Brügel's scheme:-

| | | | | | | | | | |
|-------|---|----|----|-------|----|---|---|----|----|
| m_L | 1 | 0 | -1 | | 2 | 1 | 0 | -1 | -2 |
| M_L | 2 | 1 | 0 | | 1 | | 1 | 0 | -1 |
| M_L | 1 | 0 | -1 | | 0 | | | 0 | |
| M_L | 0 | -1 | -2 | | -1 | | | | |
| | 1 | 1 | 1 | m_L | | | | | |

for $S = 1, M_L = 1, 0, -1, L = 1$
 $J = |L + S| = 0, 1, 2$

3 $P_{0,1,2}$

for $S = 0, M_L = 2, 0, -1, -2, L = 2$
 $M_L = 0 \quad L = 0$

$S = 0, L = 0, J = 0$

$S = 0, L = 2, J = 2$

The term value for $(np)^2$ electron

is $^1S_0, ^3P_{0,1,2}, ^1D_2$

Question :- Determine the term values for $(np)^4$